

# On Strongly Infinitely Divisible Matrices

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Roots of a nonnegative matrix (if they exist) may or may not be nonnegative. The matrix exponential  $A = e^B$  of an (essentially) nonnegative matrix  $B$  is indeed a nonnegative invertible matrix and all of whose nonnegative powers  $A^t = e^{tB}$  ( $t \geq 0$ ) are clearly also nonnegative. The converse is also true, as shown recently by Van-Brunt. If  $A$  is an invertible nonnegative matrix all of whose roots exist and are also nonnegative, there exists a nonnegative matrix  $B$  such that  $A = e^B$ . We refer to such an  $A$  as a strongly infinitely divisible matrix ( $A \in \mathbf{SIDM}$ ). An inverse  $M$ -matrix is a particular example of an  $\mathbf{SIDM}$ . Inverse  $M$ -matrices play an important role in this study.

Properties and connections of  $\mathbf{SIDM}$ 's to other matrix classes is still under consideration. In my talk we will discuss certain operations that leave  $\mathbf{SIDM}$  invariant, examine submatrices of  $\mathbf{SIDM}$ 's, discover an intimate connection of  $\mathbf{SIDM}$ 's and their roots to P-matrices and eventually nonnegative matrices. Further, we will discuss Hadamard/Kronecker products of  $\mathbf{SIDM}$ 's, monotonicity of roots of  $\mathbf{SIDM}$ 's and eigenvalues of  $\mathbf{SIDM}$ 's.