I will explain the useful PDE trick of making a log change of variables, and then discuss connections with Riccati equations in ODE theory. This point of view then leads to some interesting conjectures (and a little progress towards proving them) concerning the PDE approach to weak KAM theory.